



Daffodil International University

Faculty of Science & Information Technology
Department of Computing and Information System
Final Examination, Summer-2025

Course Code: MAT101, Course Title: Mathematics I

Level: 1 Term: 2

Exam Duration: 2 Hours

Marks: 40

Answer ALL Questions

[The figures in the right margin indicate the full marks and corresponding course outcomes. All portions of each question must be answered sequentially.]

1.	<p>An aerospace company is evaluating the daily operating cost of a prototype jet engine as a function of its thrust setting. Let x be the thrust level in units of 10,000 lbf (pounds-force). Based on fuel burn, thermal stress on components, and maintenance scheduling, the daily cost $C(x)$ (in thousands of dollars) of running the engine at thrust x is modeled by</p> $C(x) = x^6 - 12x^5 + 36x^4 + 4$ <p>i. Construct $C'(x)$ and find all the critical points. ii. Find the maximum and minimum daily cost of running the jet engine.</p>	[5]	CLO3 L-1,5
2.	<p>a) Simplify $\frac{7x-25}{(x-3)(x-4)}$ into partial fraction.</p> <p>b) Apply the concept of partial fraction to evaluate $\int \frac{dx}{x^3+1}$</p>	[4] [6]	CLO4 L-3,4
3.	<p>Solve the following integrations:</p> <p>i. $\int \frac{4x \, dx}{\sqrt{2x^2+1}}$</p> <p>ii. $\int x^2 e^{3x} \, dx$</p> <p>iii. $\int \frac{e^x - 1}{e^x + 1} \, dx$</p>	[3] + [3] + [4]	CLO4 L-3
4.	<p>a) Evaluate the integration the function $\sec^3 \theta$ within the interval 0 to $\frac{\pi}{4}$</p> <p>b) Find the area of the largest region bounded by the circle $x^2 + y^2 = 16$ and the straight line $x - 2 = 0$.</p>	[5] [5]	CLO4 L-1,4
5.	<p>A warehouse worker uses a hand truck to move a heavy crate along the floor. The combined displacement of the crate can be described by the vector</p> $\vec{r} = 3\hat{i} + 2\hat{j} - 5\hat{k} \text{ (In meters)}$ <p>During this move, the worker applies a steady force</p> $\vec{F} = 2\hat{i} - \hat{j} - \hat{k} \text{ (In newtons)}$ <p>Demonstrate the work done (in joules) by the worker in moving the crate along the given displacement.</p>	[5]	CLO4 L-2